

Post-Quantum Crypto is Coming!

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@Hack, Riyadh, KSA – 2021-11-28

TAURUS \rightleftharpoons

Background

Co-founder & chief security officer of Taurus SA

- Swiss firm founded in 2018, team of 35+
- Taurus used by all types of banks and financial institutions
- Crypto custody technology and infrastructure, FINMA licensed

https://taurushq.com https://t-dx.com

Expert in cryptography and security

- 15 years in crypto and security, EPFL PhD
- Designed algorithms used in Linux, Bitcoin, etc.
- Author of reference books in the field

https://aumasson.jp.https://twitter.com/veorg





★★★★☆ ~ 218







Prerequisites

Fundamental Equations

Schrödinger equation:

Time independent Schrödinger equation:

 $H\psi = E$

Standard Hamiltonian:

H

Time dependence of an expectation value:

 $rac{d\langle Q
angle}{dt}$

Generalized uncertainty principle:

 $\sigma_A \sigma$

$$i\hbar \frac{\partial \Psi}{\partial t} = H\Psi$$

$$E\psi, \qquad \Psi = \psi e^{-iEt/\hbar}$$

$$V = -\frac{\hbar^2}{2m}\nabla^2 + V$$

$$=\frac{i}{\hbar}\left\langle \left[H,Q\right]\right\rangle +\left\langle \frac{\partial Q}{\partial t}\right\rangle$$

$$\sigma_B \ge \left|\frac{1}{2i}\left< [A,B] \right>\right|^2$$





Why Quantum Computers?

Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

Not to Break Crypto..

5. CAN QUANTUM SYSTEMS BE PROBABILISTICALLY SIMULATED BY A CLASSICAL COMPUTER?

Now the next question that I would like to bring up is, of course, the interesting one, i.e., Can a quantum system be probabilistically simulated by a classical (probabilistic, I'd assume) universal computer? In other words, a computer which will give the same probabilities as the quantum system does. If you take the computer to be the classical kind I've described so far, (not the quantum kind described in the last section) and there're no changes in any laws, and there's no hocus-pocus, the answer is certainly, No! This is called the hidden-variable problem: it is impossible to represent the results of quantum mechanics with a classical universal device. To learn a little bit about it, I say let us try to put the quantum equations in a form as close as

But (Initially) to Simulate Quantum Physics

4. QUANTUM COMPUTERS—UNIVERSAL QUANTUM SIMULATORS

The first branch, one you might call a side-remark, is, Can you do it with a new kind of computer—a quantum computer? (I'll come back to the other branch in a moment.) Now it turns out, as far as I can tell, that you can simulate this with a quantum system, with quantum computer elements. It's not a Turing machine, but a machine of a different kind. If we disregard the continuity of space and make it discrete, and so on, as an approximation (the same way as we allowed ourselves in the classical case), it does seem to

Qubits Instead of Bits

Superposition state $\alpha |0\rangle + \beta |1\rangle$

are"probabilities" called amplitudes α, β (can be complex, and negative numbers)

0 with probability $|\alpha|^2$ Observation **1** with probability $|\beta|^2$



Qubits Instead of Bits

Superposition state $\alpha |0\rangle + \beta |1\rangle$

 α, β are "probabilities" called **amplitudes** (can be complex, and negative numbers)

Once observed, a qubit stays 0 or 1 forever



0 with probability $|\alpha|^2$ Observation **1** with probability $|\beta|^2$



Real randomness!

Generalizes to more than 2 states: "qutrits", "qubytes", etc.

How Quantum Algorithms Work

Circuit of quantum gates, transforming a quantum state, ending with an observation



Can be simulated with high-school linear algebra, but does no scale!

- **Quantum state** = simulated as a vector of 2^{N} amplitudes for N qubits **Quantum gates** = simulated any matrix multiplications, with $O(2^{3N})$ complexity

Quantum Speedup

When quantum computers can solve a problem faster than classical computers

Most interesting: Superpolynomial quantum speedup ("exponential" boost)



List of problems on the Quantum Zoo: <u>http://math.nist.gov/quantum/zoo/</u>

Quantum Parallelism

Quantum computers "work" on all values simultaneously, via superposition

But they cannot "try every answer in parallel and pick the best"

projection from the Hilbert space (where qubits "live") to some basis



- You can only observe one "value" that results from the interference of all, through a

NP-complete Problems

- Solution hard to find, but easy to verify
- Constraint satisfaction problems (SAT, TSP, knapsacks, etc.)
- Sometimes used in crypto (lattice problems in post-quantum schemes)

Can't be solved faster with quantum computers!



NP is not in BQP (most likely!)

BQP = bounded-error quantum polynomial time, what QC can solve efficiently



Quantum Supremacy?

Google thinks it's close to "quantum supremacy." Here's what that really means.

It's not the number of qubits; it's what you do with them that counts.

by Martin Giles and Will Knight March 9, 2018



computing terms, it's massive. This week Google unveiled Bristlecone, a new quantum computing chip

with 72 quantum bits, or qubits—the fundamental units of computation

eventy-two may not be a large number, but in quantum

Recommended Reading

QUANTUM COMPUTING SINCE DEMOCRITUS



SCOTT AARONSON

1. Atoms and the void	is even starter rate . s.t. is interview in a start . s.t.
2. Sets	and a second
3. Gödel, Turing, and friends	18
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Impact on Cryptography



Shor's Quantum Algorithm (1994)

Polynomial-time algorithm for the following problems:

- Computes **p** given $\mathbf{n} = \mathbf{pq}$
- Computes **d** given $\mathbf{y} = \mathbf{x}^d \mod \mathbf{p} \rightarrow ECC/DH$ dead

Practically impossible on a classical machine

#QuantumSpeedup

- \rightarrow RSA dead





How Bad for Crypto?



Annoying: Signatures (ECDSA, Ed25519, etc.) - Can be reissued with a post-quantum algorithm - Applications: Bitcoin, secure boot







Bad: <u>Key agreement</u> (Diffie-Hellman, ECDH, etc.) - Partially mitigated by secret internal states and reseeding - Applications: TLS, end-to-end messaging

Disaster: <u>Encryption</u> (RSA encryption, ECIES, etc.) Encrypted messages compromised forever Applications: Key encapsulation, secure enclaves

How Many Qubits



How Many Qubits

1000000

0

Linear scale

In today's QC



Hopes for the next 5 years Needed to break crypto

Quantum Computers Today

Scaling IBM Quantum technology



PS: "and beyond" might be in a long time, if ever :)



Next family of IBM Quantum systems

23	and beyond
21 qubits ndor	Path to 1 million qubits and beyond Large scale systems
advancement	Key advancement
gration	Build new infrastructure, quantum error correction

Is D-Wave a Threat to Crypto?





No, because it's not even quantum computing

- Dedicated hardware for specific optimization problems
- **Can't run Shor**, so can't break crypto. $\sqrt{(\nu)}/7$



Quantum version of simulated annealing, with no evidence of quantum speed-up

Speculative Estimates...

Designing a Million-Qubit Quantum Computer Using Resource Performance Simulator

Muhammad Ahsan, Rodney Van Meter, Jungsang Kim

(Submitted on 2 Dec 2015)

The optimal design of a fault-tolerant quantum computer involves finding an appropriate balance between the burden of large-scale integration of noisy components and the load of improving the reliability of hardware technology. This balance can be evaluated by quantitatively modeling the execution of quantum logic operations on a realistic quantum hardware containing limited computational resources. In this work, we report a complete performance simulation software tool capable of (1) searching the hardware design space by varying resource architecture and technology parameters, (2) synthesizing and scheduling fault-tolerant quantum algorithm within the hardware constraints, (3) quantifying the performance metrics such as the execution time and the failure probability of the algorithm, and (4) analyzing the breakdown of these metrics to highlight the performance bottlenecks and visualizing resource utilization to evaluate the adequacy of the chosen design. Using this tool we investigate a vast design space for implementing key building blocks of Shor's algorithm to factor a 1,024-bit number with a baseline budget of 1.5 million qubits. We show that a trapped-ion quantum computer designed with twice as many qubits and one-tenth of the baseline infidelity of the communication channel can factor a 2,048-bit integer in less than five months.

Speculative estimates...

make reliable guesses (10 scientists = 12 different predictions)

The Present and Future of Discrete Logarithm Problems on Noisy Quantum Computers

YOSHINORI AONO¹, SITONG LIU², TOMOKI TANAKA^{3,5}, SHUMPEI UNO^{4,5}, RODNEY VAN METER^{2,5} (Senior Member, IEEE), NAOYUKI SHINOHARA¹, RYO NOJIMA¹

"Predicting" quantum computers is a Bayesian game; too little information to

scenario. Their prediction is based on their quantifier of quantum devices that they named generalized logical qubits. They predicted that a superconducting quantum device capable of solving RSA-2048 (using 4,100 qubits) would be available in the early 2050s, rather than before 2039. This is more optimistic than expert opinions [38], [39] published in 2019 and updated in 2020. Mosca and Piani say that 90% of experts predict that there is 50% or greater chance of a quantum device that can break RSA-2048 in 24 hours being released in the next 20 years.



When it Looks too Good to be True..

Factoring 2048 RSA integers in 177 days with 13436 qubits and a multimode memory

Élie Gouzien^{*} and Nicolas Sangouard[†] Université Paris-Saclay, CEA, CNRS, Institut de physique théorique, 91 191 Gif-sur-Yvette, France (Dated: March 11, 2021)

We analyze the performance of a quantum computer architecture combining a small processor and a storage unit. By focusing on integer factorization, we show a reduction by several orders of magnitude of the number of processing qubits compared to a standard architecture using a planar grid of qubits with nearest-neighbor connectivity. This is achieved by taking benefit of a temporally and spatially multiplexed memory to store the qubit states between processing steps. Concretely, for a characteristic physical gate error rate of 10^{-3} , a processor cycle time of 1 microsecond, factoring a 2048 bits RSA integer is shown possible in 177 days with a processor made with 13 436 physical qubits and a multimode memory with 2 hours storage time. By inserting additional error-correction steps, storage times of 1 second are shown to be sufficient at the cost of increasing the runtime by about 23%. Shorter runtimes (and storage times) are achievable by increasing the number of qubits in the processing unit. We suggest realizing such an architecture using a microwave interface between a processor made with superconducting qubits and a multiplexed memory using the principle of photon echo in solids doped with rare-earth ions.

Introduction — Superconducting qubits form the building blocks of one of the most advanced platforms for realizing quantum computers [1]. The standard architecture consists in laying superconducting qubits in a 2D grid and making the computation using only neighboring interactions. Recent estimations showed however that fault-tolerant realizations of various quantum algorithms with this architecture would require millions physical qubits [2–4]. These performance analyses naturally raise the question of an architecture better exploiting the potential of superconducting qubits.

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Sam Jaques

Replying to @veorq

qubits"

😪 Craig Gidney @CraigGidney · Mar 15

considering a world where mem ends up cheaper than cpu.

Su Introduction —

building blocks of one

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Quantum Search

- Grover's algorithm (1996)
- **S**earches in N items in \sqrt{N} queries!
- AES-128 broken in $\sqrt{2^{128}} = 2^{64}$ operations?

Caveats behind this simplistic view:

- Constant factor in O(/N) may be huge
- Doesn't easily parallelise, as classical search does



Quantum-Searching AES Keys

	#gates			depth		
k	T	Clifford	T	overall		
128	$1.19\cdot 2^{86}$	$1.55\cdot 2^{86}$	$1.06\cdot 2^{80}$	$1.16\cdot 2^{81}$	2,953	
192	$1.81\cdot2^{118}$	$1.17\cdot2^{119}$	$1.21\cdot2^{112}$	$1.33\cdot2^{113}$	4,449	
256	$1.41\cdot2^{151}$	$1.83\cdot2^{151}$	$1.44\cdot2^{144}$	$1.57\cdot2^{145}$	6,681	

If gates are the size of a hydrogen atom (12pm) this depth is the diameter of the solar system (~10¹³m), yet less than 5 grams

No doubt more efficient circuits will be designed...

 $3, 192, 256\}.$

<u>https://arxiv.org/pdf/1512.04965v1.pdf</u>

Eliminating the Problem: 256-bit Keys



Defeating Quantum Algorithms



Aka quantum-safe, quantum-resilient

- Must not rely on factoring or discrete log problems
- Must be well-understood with respect to quantum



log problems t to quantum

Why Bother?

Insurance against QC threat:

- "QC has a probability p work in year X and the impact would be \$N for us" "I'd like to eliminate this risk and I'm ready to spend \$M for it"

Supposedly the motivation of USG/NSA:

future." — NSA in CNSS advisory 02-2015





- "we anticipate a need to shift to quantum-resistant cryptography in the near

NSA's Take (Aug 2021)

Q: Is NSA worried about the threat posed by a potential quantum computer because a CRQC exists? A: NSA does not know when or even if a quantum computer of sufficient size and power to exploit public key cryptography (a CRQC) will exist.

Q: Why does NSA care about quantum computing today? Isn't quantum computing a long way off? A: The cryptographic systems that NSA produces, certifies, and supports often have very long lifecycles. NSA has to produce requirements today for systems that will be used for many decades in the future, and data protected by these systems will still require cryptographic protection for decades after these solutions are replaced. There is growing research in the area of quantum computing, and global interest in its pursuit have provoked NSA to ensure the enduring protection of NSS by encouraging the development of post-quantum cryptographic standards and planning for an eventual transition.

Q: What are the timeframes in NSS for deployment of new algorithms, use of equipment, and national security information intelligence value?

A: New cryptography can take 20 years or more to be fully deployed to all National Security Systems. NSS equipment is often used for decades after deployment. National security information intelligence value varies depending on classification, sensitivity, and subject, but it can require protection for many decades.

https://media.defense.gov/2021/Aug/04/2002821837/-1/-1/1/Quantum FAQs 20210804.pdf

"Hey NIST we Need Crypto Standards"

CSRC HOME > GROUPS > CT > POST-QUANTUM CRYPTOGRAPHY PROJECT

POST-QUANTUM CRYPTO PROJECT

NEWS -- August 2, 2016: The National Institute of Standards and Technology (NIST) is requesting comments on a new process to solicit, evaluate, and standardize one or more quantum-resistant public-key cryptographic algorithms. Please see the Post-Quantum Cryptography Standardization menu at left.

Fall 2016	Formal Call for Proposals
Nov 2017	Deadline for submissions
Early 2018	Workshop - Submitter's Presentations
3-5 years	Analysis Phase - NIST will report findings 1-2 workshops during this phase
2 years later	Draft Standards ready

Submission of post-quantum algorithms for:

- Signature
- Encryption and key agreement, via key encapsulation mechanisms (KEM)

Post-Quantum Cryptography Standardization

The <u>Round 3 candidates</u> were announced July 22, 2020. <u>NISTIR 8309</u>, Status Report on the Second Round of the NIST Post-Quantum Cryptography Standardization Process is now available. NIST has developed <u>Guidelines for Submitting Tweaks</u> for Third Round Finalists and Candidates.





The Five Families

- Based on coding theory (McEliece, Niederreiter):
 - Solid foundations from the late 1970s, large keys, encryption only
- Based on multivariate polynomials evaluation
 - Based on multivariate equations' hardness, mostly for signatures
- Based on hash functions and tree-based constructions
 - Ideas from the 70s, as secure as the hash, large keys, signature only
- Based on elliptic curve isogenies
 - More recent problem, relatively slow, Diffie-Hellman-like key agreement
- Based on *lattice problems...*

Lattice-Based Crypto: Intuition

Based on problems such as **learning with errors** (LWE):

- S a secret vector of numbers modulo q
- Receive pairs (A, B)
 - $A = (A_0, ..., A_{n-1})$ is a vector of uniformly random numbers
 - $\mathbf{B} = \langle \mathbf{S}, \mathbf{A} \rangle + \mathbf{E}$, a vector of $\mathbf{B}_i = \mathbf{S}_i^* \mathbf{A}_i + \mathbf{E}_i$
 - $E = (E_0, ..., E_{n-1})$ is an **unknown** vector or *normal*-random numbers

Attacker goal: find **S** given many pairs (**A**, **B**)

Without E: trivial (linear systems of equations)

With E: NP-hard

Lattice-Based Crypto: Future Standards

The best balance between performance and security assurance

Heated discussions about their relative merits, and speculative theories.

NIST Round 3

Code-based:

Classic McEliece (KEM, finalist)

Lattice-based:

- Dilithium (signature, finalist)
- Falcon (signature, finalist)
- Kyber (KEM, finalist)
- NTRU (KEM, finalist)
- SABER (KEM, finalist)

MQ-based:

Rainbow (signature, finalist)



See analyses at <u>https://ntruprime.cr.yp.to/warnings.html</u>

e data points 657 views	[CFRG] NSA vs. hybrid
Oct 20, 2021,	D. J. Bernstein <u>via</u> ietf.org Fri, to cfrg ▼
n to assume that Kyber is the most efficient vever, if I want an ARM Cortex-M4 to decrypt core-SVP >= 2^128, then my costs (sorted s follows, according to (1) pqm4 benchmarks og/pgm4/blob/master/benchmarks.md. (2) tables	This looks to me like something that should be discussed in CFRG rather than LAMPS: <u>https://datatracker.ietf.org/meeting/112/materials/slides-112-lamps-hybrid https://mailarchive.ietf.org/arch/msg/spasm/McksDhejGgJJ6xG617FEWI</u>
mit.edu Oct 30, 2021, 11:41:37 PM 🟠 🌾 🗄	This is one part of a big push by NSA across multiple non-CFRG venues to convince everyone to
ing reply, I didn't see a straight answer to my question about the im from the end of your talk of 10+ weeks ago, namely:	* deploy small lattice systemswhich _hopefully_ protects against quantum computersand
	* _turn off ECCthis is the scary part, since there's a serious
central question is this: is this claim still in effect, and if so, when can the pect to see it substantiated?	risk that the small lattice systems are easier to break than ECC.
arkable claim, one would normally expect to see a research paper nd before so much time has passed.	





Hash-Based Crypto: Intuition

- "One-time signatures", Lamport, **1979**:
- 1. Generate a key pair
 - Pick random strings K_0 and K_1 (your **private key**)
 - The public key is the two values $H(K_0)$, $H(K_1)$
- 2. To sign the bit 0, show K_0 , to sign 1 show K_1

Problems

- Need as many keys as there are bits
- A key can only be used once
- Solution: more hashing, and trees!



Hash Crypto: Sign More than 0 and 1 Winternitz, **1979**:

- 1. Public key is $H(H(H(H(H(\dots (K)\dots)) = H^w(K))))$ (w times)
- 2. To sign a number x in [0; w 1], compute S=H^x(K) Verification: check that $H^{w-x}(S) = public key$
- A key must still be used only once

Hash Crypto: From One-Time to Many-Time

"Compress" a list of one-time keys using a hash tree





Hash Crypto: From One-Time to Many-Time

When a new **one-time public key K** $_i$, is used...

... give its authentication path to the root pub key (aka proof of membership)





PQC Performance

Algorithm	Public key (bytes)	$\begin{array}{c} \mathbf{Ciphertext} \\ (\mathrm{bytes}) \end{array}$	Key gen. (ms)	Encaps. (ms)	$\begin{array}{c} \mathbf{Decaps.}\\ (\mathrm{ms}) \end{array}$	-
ECDH NIST P-256	64	64	0.072	0.072	0.072	Elliptic curves (not post-quantum)
SIKE p434	330	346	13.763	22.120	23.734	Isogeny-based
Kyber 512-90s	800	736	0.007	0.009	0.006	Lattian hanad
FrodoKEM-640-AES	9,616	9,720	1.929	1.048	1.064	Lattice-based

Table 1: Key exchange algorithm communication size and runtime

Algorithm	Public key (bytes)	Signature (bytes)	$\frac{\mathbf{Sign}}{(\mathrm{ms})}$	$\begin{array}{c} \mathbf{Verify} \\ (\mathrm{ms}) \end{array}$
ECDSA NIST P-256	64	64	0.031	0.096
Dilithium2	$1,\!184$	$2,\!044$	0.050	0.036
qTESLA-P-I	$14,\!880$	$2,\!592$	1.055	0.312
Picnic-L1-FS	33	$34,\!036$	3.429	2.584

Table 2: Signature scheme communication size and runtime

From "Benchmarking Post-Quantum Cryptography in TLS" https://eprint.iacr.org/2019/1447



Using PQC Today

Libraries, implementations, specifications (for TLS, IPsec), standards

See https://github.com/veorq/awesome-post-quantum

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<> Code	Issues 19	Pull requests 4	Actions	Projects 0		P by
C library fo	C library for quantum-safe cryptography. https://openquantumsafe.org/					Co

PQClean / PQClean	📮 mupq / pqm4	
Code Issues 19 In Pull requests 3 Actions Projects 0	Code Issues 3 Pull requests 0 Actions	C Pqshield.com
Clean, portable, tested implementations of post-quantum cryptography	Post-quantum crypto library for the ARM Cortex-M4	SHIEL

WS Security Blog

Post-quantum TLS now supported in AWS KMS

/ Andrew Hopkins | on 04 NOV 2019 | in Advanced (300), AWS Key Management Service, Security, Identity, & ompliance | Permalink | 🗩 Comments | 🏞 Share





Conclusion

Quantum computers are not here yet, and nobody knows when they'll be

QUANTUM COMPUTING | OPINION

Will Quantum Computing Ever Live **Up to Its Hype?**

One expert warns that the field is overpromising, while another says his firm is on the verge of building "useful" machines

https://www.scientificamerican.com/article/will-quantum-computing-ever-live-up-to-its-hype/

Post-quantum crypto is being standardised and deployed, as an insurance

See learning resources on https://github.com/veorg/awesome-post-quantum

Exciting research and engineering, but *no practical value yet*, beware the FUD



TAURUS $\Box \quad \bigcirc \quad \overleftarrow{}$

شکرا ^{*} Thank you -

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